

Учебная практика 2 курсы

Исследовать на сходимость и равномерную сходимость функциональный ряд на множествах E_1 и E_2 .

$$1. \sum_{k=1}^{\infty} \operatorname{arctg} \frac{x}{k^2} \quad E_1 = [0; 1] \quad E_2 = [0; +\infty)$$

$$2. \sum_{k=1}^{\infty} \frac{1}{1+k^2x} \quad E_1 = (0; 1] \quad E_2 = [1; +\infty)$$

$$3. \sum_{k=1}^{\infty} e^{-k \arcsin x} \quad E_1 = (0; \frac{1}{2}) \quad E_2 = (\frac{1}{2}; 1]$$

$$4. \sum_{k=1}^{\infty} \operatorname{arctg} \frac{1}{k^2x} \quad E_1 = (0; 1] \quad E_2 = (1; +\infty)$$

$$5. \sum_{k=1}^{\infty} \ln(1 + \frac{1}{k^2x}) \quad E_1 = (0; 1) \quad E_2 = [1; 2]$$

$$6. \sum_{k=1}^{\infty} x e^k \sin \frac{x}{5k} \quad E_1 = (0; 1) \quad E_2 = (1; +\infty)$$

$$7. \sum_{k=1}^{\infty} 2^k \operatorname{tg} \frac{1}{3^k - x + 1} \quad E_1 = (0; 1) \quad E_2 = (1; +\infty)$$

$$8. \sum_{k=1}^{\infty} \frac{e^{-kx}}{x \sqrt{k}} \quad E_1 = (0; 1) \quad E_2 = (1; +\infty)$$

$$9. \sum_{k=1}^{\infty} \frac{\sin kx}{e^{k^2x}} \quad E_1 = (1; +\infty) \quad E_2 = (0; +\infty)$$

$$10. \sum_{k=1}^{\infty} \frac{\sqrt{x}}{k^2} \sin \frac{x}{k^2} \quad E_1 = (0; 1) \quad E_2 = (0; +\infty)$$

$$11. \sum_{k=1}^{\infty} \frac{\sin kx}{e^{k^2x} - 1} \quad E_1 = (1; +\infty) \quad E_2 = (0; +\infty)$$

$$12. \sum_{k=1}^{\infty} \sqrt{\frac{k}{x}} \sin \frac{x}{4k^2} \quad E_1 = (0; 1) \quad E_2 = (1; +\infty)$$

$$13. \sum_{k=1}^{\infty} \frac{x}{k} e^{3k - (k-x)^2} \quad E_1 = (0; 1) \quad E_2 = (1; +\infty)$$

$$14. \sum_{k=1}^{\infty} \sqrt{\frac{x}{k}} \frac{\sin kx}{1+kx} \quad E_1 = (0; 1) \quad E_2 = (1; +\infty)$$

$$15. \sum_{k=1}^{\infty} \frac{x^3 \sqrt[6]{k}}{x^3 + k} \sin \frac{x}{\sqrt[3]{k}} \quad E_1 = (0; 1) \quad E_2 = (1; +\infty)$$

$$16. \sum_{k=1}^{\infty} x^2 e^{-kx^2} \quad E_1 = (1; +\infty) \quad E_2 = (0; +\infty)$$

$$17. \sum_{k=1}^{\infty} \frac{x}{\sqrt{k}} e^{-x^2 k} \quad E_1 = (1; +\infty) \quad E_2 = (0; +\infty)$$

$$18. \sum_{k=1}^{\infty} \frac{x}{x + k^2} \sin \frac{k^2}{x} \quad E_1 = (0; 1) \quad E_2 = (1; +\infty)$$

$$19. \sum_{k=1}^{\infty} \frac{1}{k+x} (e^{\frac{x}{k}} - 1) \quad E_1 = (0; 1) \quad E_2 = (1; +\infty)$$

$$20. \sum_{k=1}^{\infty} \frac{k^2 \sqrt[4]{x}}{x + k^2} \operatorname{arctg} \sqrt{\frac{x}{k^3}} \quad E_1 = (0; 1) \quad E_2 = (1; +\infty)$$

$$21. \sum_{k=1}^{\infty} x e^{-k^2 x^2} \operatorname{arctg} kx \quad E_1 = (0; 1) \quad E_2 = (1; +\infty)$$

$$22. \sum_{k=1}^{\infty} \frac{k^2}{x} e^{-\frac{k^2}{x}} \quad E_2 = (0; +\infty) \quad E_2 = (0; 1)$$

$$23. \sum_{k=1}^{\infty} \frac{1}{\sqrt{k}} \ln \frac{k+x}{k} \quad E_1 = (0; 1) \quad E_2 = (1; +\infty)$$

$$24. \sum_{k=1}^{\infty} x^2 2^k \operatorname{tg} \frac{x}{4^k} \quad E_1 = (0; 1) \quad E_2 = (1; +\infty)$$

$$25. \sum_{k=1}^{\infty} \frac{x}{x^2 - kx + k^2} \quad E_1 = (0; 1) \quad E_2 = (1; +\infty)$$