

ЗАДАНИЕ №2, 1-й курс 02.03.01

Даны две системы векторов a_1, a_2, a_3, a_4 и b_1, b_2, b_3 пространства \mathbb{R}^4 , на которые натянуты линейные подпространства L_1 и L_2 соответственно.

1) Найти максимальную линейно независимую подсистему системы векторов a_1, a_2, a_3, a_4 и выразить все векторы системы линейно через векторы найденной подсистемы;

2) Показать, что b_1, b_2, b_3 - базис подпространства L_2 и найти координаты вектора c в этом базисе;

3) Найти базис пересечения подпространств L_2 и L_1 ;

4) Найти базис какого-нибудь подпространства L , для которого выполняется равенство $\mathbb{R}^4 = (L_1 \cap L_2) \oplus L$

$$1. \quad a_1 = \{0, -1, 0, 0\}, a_2 = \{1, 2, 0, -1\}, a_3 = \{-2, 2, -1, -1\}, a_4 = \{0, -1, -1, -1\}, \\ b_1 = \{2, 2, -1, 2\}, b_2 = \{2, 2, -1, -1\}, b_3 = \{0, -2, -2, -1\}$$

$$2. \quad a_1 = \{2, 2, 1, 1\}, a_2 = \{-2, 0, -1, -2\}, a_3 = \{-1, 0, 0, -2\}, a_4 = \{2, -1, 0, -1\}, \\ b_1 = \{0, -2, -2, 2\}, b_2 = \{-1, -1, 2, 2\}, b_3 = \{1, 1, 0, 2\}$$

$$3. \quad a_1 = \{-2, 0, 0, 2\}, a_2 = \{2, 1, 0, -2\}, a_3 = \{-2, 1, -2, -2\}, a_4 = \{0, 1, 1, 0\}, \\ b_1 = \{2, 1, 1, 0\}, b_2 = \{0, 0, 0, 0\}, b_3 = \{1, -2, 0, 0\}$$

$$4. \quad a_1 = \{0, 1, 1, -1\}, a_2 = \{0, 0, -1, -2\}, a_3 = \{1, 0, 0, 2\}, a_4 = \{1, 1, 1, 1\}, \\ b_1 = \{1, -1, -1, -2\}, b_2 = \{2, 0, -1, -2\}, b_3 = \{2, 0, 2, 1\}$$

$$5. \quad a_1 = \{2, -2, 1, -1\}, a_2 = \{-2, 1, 2, -2\}, a_3 = \{-1, -2, -2, 1\}, a_4 = \{0, 1, 1, 2\}, \\ b_1 = \{1, 1, -1, 1\}, b_2 = \{0, -2, 2, 2\}, b_3 = \{1, -1, -1, 1\}$$

$$6. \quad a_1 = \{0, -2, 1, 1\}, a_2 = \{0, 0, -2, 1\}, a_3 = \{2, 1, -2, 1\}, a_4 = \{2, 1, -1, -1\}, \\ b_1 = \{1, 0, 2, 1\}, b_2 = \{1, 1, 2, 0\}, b_3 = \{1, -1, 0, -1\}$$

$$7. \quad a_1 = \{1, -1, 1, -1\}, a_2 = \{2, -1, 2, -1\}, a_3 = \{2, -1, 2, 0\}, a_4 = \{-2, -1, -1, 0\}, \\ b_1 = \{1, 0, -2, 1\}, b_2 = \{1, 0, 2, -1\}, b_3 = \{2, -2, -1, 2\}$$

$$8. \quad a_1 = \{2, 1, 1, -1\}, a_2 = \{-1, -1, 1, 2\}, a_3 = \{1, -2, -1, 2\}, a_4 = \{1, 0, -1, -1\}, \\ b_1 = \{1, -1, 2, 0\}, b_2 = \{2, 1, 1, -1\}, b_3 = \{-1, 1, -2, -2\}$$

$$9. \quad a_1 = \{0, 1, 0, 1\}, a_2 = \{2, 1, 1, -1\}, a_3 = \{-2, 1, 2, -1\}, a_4 = \{0, 2, -1, -1\}, \\ b_1 = \{0, -1, 0, 2\}, b_2 = \{-2, 1, 1, 2\}, b_3 = \{0, 2, 0, -1\}$$

$$10. \quad a_1 = \{-2, 1, 1, 2\}, a_2 = \{1, 1, -1, -2\}, a_3 = \{-1, -2, 1, -1\}, a_4 = \{2, 1, 1, 2\}, \\ b_1 = \{-1, 2, 1, 0\}, b_2 = \{-2, 0, 1, 2\}, b_3 = \{2, -1, -2, 0\}$$

$$11. \quad a_1 = \{-1, 2, -1, -2\}, a_2 = \{0, 0, 1, 2\}, a_3 = \{2, 1, 0, 1\}, a_4 = \{1, 1, 0, -1\}, \\ b_1 = \{2, 2, 1, 2\}, b_2 = \{-1, 0, -1, 1\}, b_3 = \{2, -2, 2, -2\}$$

$$12. \quad a_1 = \{2, 2, -1, 2\}, a_2 = \{-1, -2, 0, 2\}, a_3 = \{0, -1, -2, 1\}, a_4 = \{0, -2, 2, -2\}, \\ b_1 = \{-2, -1, 0, -1\}, b_2 = \{-1, -2, -1, -2\}, b_3 = \{1, 2, 1, 2\}$$

$$13. \quad a_1 = \{0, 2, 1, -1\}, a_2 = \{0, 0, -1, 1\}, a_3 = \{-2, -1, 1, -2\}, a_4 = \{-1, -1, -1, -2\}, \\ b_1 = \{1, 1, 2, 2\}, b_2 = \{2, -1, 2, -1\}, b_3 = \{-1, 1, 1, 2\}$$

14. $a_1 = \{-2, 0, 0, 1\}, a_2 = \{2, 2, -1, 2\}, a_3 = \{-1, 0, 1, -2\}, a_4 = \{-1, 2, 1, 2\},$
 $b_1 = \{-2, 0, 0, -2\}, b_2 = \{2, -2, -2, 2\}, b_3 = \{-1, 0, -1, 1\}$
15. $a_1 = \{0, -1, -1, 1\}, a_2 = \{2, 2, -1, 0\}, a_3 = \{2, 1, 2, -1\}, a_4 = \{1, -1, -2, 0\},$
 $b_1 = \{0, 2, -1, 0\}, b_2 = \{2, 1, -2, -2\}, b_3 = \{1, -2, 0, 0\}$
16. $a_1 = \{-1, 0, -1, -1\}, a_2 = \{2, 0, -2, -1\}, a_3 = \{0, 0, 2, -2\}, a_4 = \{2, -2, 0, 0\},$
 $b_1 = \{-1, -2, -1, 2\}, b_2 = \{2, -2, -1, -2\}, b_3 = \{2, 0, 2, -1\}$
17. $a_1 = \{0, 1, 1, -1\}, a_2 = \{0, -1, 2, 1\}, a_3 = \{1, 0, -2, 2\}, a_4 = \{0, 2, -2, 0\},$
 $b_1 = \{-1, -1, 2, -2\}, b_2 = \{-2, 2, 0, 2\}, b_3 = \{-1, 2, 1, 2\}$
18. $a_1 = \{-1, 1, 0, -2\}, a_2 = \{0, -1, -2, 1\}, a_3 = \{2, 2, -1, 0\}, a_4 = \{-1, 2, 0, -1\},$
 $b_1 = \{1, -1, -1, -2\}, b_2 = \{-1, -2, 2, -2\}, b_3 = \{-1, 2, 1, 2\}$
19. $a_1 = \{1, -2, -2, 0\}, a_2 = \{0, 2, 1, 0\}, a_3 = \{2, 0, -1, -2\}, a_4 = \{-1, 1, 0, 1\},$
 $b_1 = \{0, 0, 1, -2\}, b_2 = \{1, 2, -1, -2\}, b_3 = \{1, 2, -2, 1\}$
20. $a_1 = \{-2, 0, -1, -1\}, a_2 = \{-2, -2, 0, 0\}, a_3 = \{2, 0, -2, 1\}, a_4 = \{0, -1, -1, 1\},$
 $b_1 = \{-2, 0, -1, 2\}, b_2 = \{1, -2, 0, -1\}, b_3 = \{-2, -1, -1, 1\}$
21. $a_1 = \{-1, 0, 0, 0\}, a_2 = \{-2, 0, 0, 2\}, a_3 = \{2, 2, 0, 2\}, a_4 = \{-1, -2, 2, 2\},$
 $b_1 = \{0, -2, -1, 0\}, b_2 = \{-1, 0, -1, -1\}, b_3 = \{2, 2, -1, -2\}$
22. $a_1 = \{-1, -2, -1, 1\}, a_2 = \{-2, 2, -2, 2\}, a_3 = \{-1, 2, 0, 0\}, a_4 = \{-1, -2, 0, -1\},$
 $b_1 = \{-1, -1, -1, 2\}, b_2 = \{0, -1, 2, 1\}, b_3 = \{-1, 2, 1, 1\}$
23. $a_1 = \{0, -2, 2, 2\}, a_2 = \{2, 1, -1, 0\}, a_3 = \{2, 2, 2, 0\}, a_4 = \{1, -2, 2, 0\},$
 $b_1 = \{0, 0, -1, 0\}, b_2 = \{2, -1, -2, -1\}, b_3 = \{-1, -1, 0, 2\}$
24. $a_1 = \{-2, 0, -1, 1\}, a_2 = \{-1, -2, -1, 0\}, a_3 = \{1, -2, 1, -1\}, a_4 = \{2, -2, 1, -1\},$
 $b_1 = \{-2, -2, 0, 2\}, b_2 = \{-2, 2, -1, 1\}, b_3 = \{2, -1, -2, 0\}$
25. $a_1 = \{-1, -1, 0, 2\}, a_2 = \{-1, 2, 2, -1\}, a_3 = \{2, -1, 1, -1\}, a_4 = \{2, 0, 1, 1\},$
 $b_1 = \{-2, -2, -2, 2\}, b_2 = \{0, 0, 1, -1\}, b_3 = \{1, -1, -2, 1\}$
26. $a_1 = \{1, 1, 2, 1\}, a_2 = \{0, 1, 1, 1\}, a_3 = \{2, 1, 1, 1\}, a_4 = \{1, -1, 0, 0\},$
 $b_1 = \{1, -1, -1, 1\}, b_2 = \{-1, -1, -2, 0\}, b_3 = \{1, 1, 1, -1\}$
27. $a_1 = \{0, 1, -1, 1\}, a_2 = \{0, 2, 2, -1\}, a_3 = \{-1, 1, 2, 1\}, a_4 = \{-1, 2, 1, 0\},$
 $b_1 = \{1, 2, 2, 2\}, b_2 = \{-2, 2, 2, -1\}, b_3 = \{0, -2, 1, -2\}$
28. $a_1 = \{0, 1, 1, 2\}, a_2 = \{-1, 2, 1, 0\}, a_3 = \{-2, 1, 0, 2\}, a_4 = \{2, -2, 2, -2\},$
 $b_1 = \{2, -2, 2, -2\}, b_2 = \{1, 0, 1, -2\}, b_3 = \{-2, 2, 0, 1\}$
29. $a_1 = \{2, 2, 0, 2\}, a_2 = \{2, -1, 2, -1\}, a_3 = \{2, 0, 1, -2\}, a_4 = \{-1, 2, 0, -1\},$
 $b_1 = \{0, 1, 1, -2\}, b_2 = \{-2, 0, 2, -2\}, b_3 = \{-2, -2, 0, -2\}$
30. $a_1 = \{1, -2, 2, 1\}, a_2 = \{1, 2, -2, 1\}, a_3 = \{1, -2, -2, -1\}, a_4 = \{-1, -2, -2, -2\},$
 $b_1 = \{1, -2, -2, 0\}, b_2 = \{2, 2, -1, -2\}, b_3 = \{-2, -2, -2, 0\}$
31. $a_1 = \{1, -2, 2, -2\}, a_2 = \{-1, 1, -2, 0\}, a_3 = \{1, 0, 0, -2\}, a_4 = \{1, 2, 0, -1\},$
 $b_1 = \{-1, 1, -1, 0\}, b_2 = \{1, 0, 1, 0\}, b_3 = \{-2, 2, -1, 0\}$

32. $a_1 = \{2, -2, -1, 1\}, a_2 = \{-1, 2, -2, -2\}, a_3 = \{-2, -1, 0, -2\}, a_4 = \{-1, -2, -2, -1\},$
 $b_1 = \{0, -2, 0, -2\}, b_2 = \{2, -1, 1, -2\}, b_3 = \{1, -2, 1, 1\}$
33. $a_1 = \{-2, -2, 2, -2\}, a_2 = \{0, 1, -2, 0\}, a_3 = \{-1, -1, 0, 0\}, a_4 = \{-2, -2, 1, 1\},$
 $b_1 = \{2, 1, -1, -1\}, b_2 = \{1, 0, -1, -1\}, b_3 = \{0, 1, 1, 2\}$
34. $a_1 = \{-1, 0, 1, -1\}, a_2 = \{1, -2, 0, -2\}, a_3 = \{2, 2, 2, 1\}, a_4 = \{-2, -2, -1, -2\},$
 $b_1 = \{1, 1, -1, -1\}, b_2 = \{-1, 1, 1, 1\}, b_3 = \{1, -2, 2, 2\}$
35. $a_1 = \{-1, 2, 1, -1\}, a_2 = \{-2, 2, -1, -2\}, a_3 = \{-1, -2, -2, -2\}, a_4 = \{1, -1, 2, 1\},$
 $b_1 = \{-1, 1, -1, 2\}, b_2 = \{-1, 2, 1, -2\}, b_3 = \{1, 0, -2, 2\}$
36. $a_1 = \{1, 0, 2, 1\}, a_2 = \{2, -1, -1, -2\}, a_3 = \{-2, -2, 2, -2\}, a_4 = \{2, -2, 0, 1\},$
 $b_1 = \{1, 1, -2, 0\}, b_2 = \{2, -2, -1, 1\}, b_3 = \{-2, -1, 2, 0\}$
37. $a_1 = \{1, -1, 0, -2\}, a_2 = \{2, 1, -2, -2\}, a_3 = \{0, -2, 0, -1\}, a_4 = \{-2, 0, 1, 1\},$
 $b_1 = \{1, 0, -2, -2\}, b_2 = \{1, 2, 2, -1\}, b_3 = \{-2, 1, 0, 1\}$
38. $a_1 = \{2, 2, -2, -2\}, a_2 = \{2, 1, -2, 2\}, a_3 = \{0, 1, -2, 0\}, a_4 = \{-2, 0, 2, 1\},$
 $b_1 = \{1, -2, 0, 1\}, b_2 = \{0, 1, 1, 2\}, b_3 = \{2, 0, -2, -1\}$
39. $a_1 = \{0, -1, 2, -2\}, a_2 = \{2, 1, 1, -1\}, a_3 = \{-2, -2, 2, -2\}, a_4 = \{0, 0, 1, 2\},$
 $b_1 = \{-2, -1, -2, 1\}, b_2 = \{-2, 2, 0, 2\}, b_3 = \{-2, 2, -2, 1\}$
40. $a_1 = \{2, -1, -1, 2\}, a_2 = \{2, 1, 2, 0\}, a_3 = \{2, 0, -2, 1\}, a_4 = \{-2, -2, 0, -2\},$
 $b_1 = \{1, 0, -2, -2\}, b_2 = \{0, 1, -2, -2\}, b_3 = \{0, -2, 0, 0\}$
41. $a_1 = \{-1, -2, -2, 2\}, a_2 = \{0, -2, 2, 2\}, a_3 = \{1, -1, 1, -2\}, a_4 = \{-1, 0, 1, -2\},$
 $b_1 = \{0, 1, 0, -2\}, b_2 = \{-2, -2, -1, 0\}, b_3 = \{1, -1, 1, 1\}$
42. $a_1 = \{-1, -2, -1, 2\}, a_2 = \{1, 0, 0, -1\}, a_3 = \{1, 1, -1, -1\}, a_4 = \{-1, 1, -1, 2\},$
 $b_1 = \{0, -2, -2, -2\}, b_2 = \{1, 1, 0, 1\}, b_3 = \{-2, 1, 1, 0\}$
43. $a_1 = \{-2, -2, 1, 1\}, a_2 = \{0, -2, 2, 0\}, a_3 = \{-2, 0, -2, 0\}, a_4 = \{-2, 1, 2, 2\},$
 $b_1 = \{-1, 2, -2, 1\}, b_2 = \{2, 2, 2, 2\}, b_3 = \{2, 2, 0, 2\}$
44. $a_1 = \{0, 1, 1, 2\}, a_2 = \{0, -1, 2, -1\}, a_3 = \{-1, 1, 2, 1\}, a_4 = \{1, 1, 2, -1\},$
 $b_1 = \{-2, -1, -2, 2\}, b_2 = \{0, -1, -2, 1\}, b_3 = \{2, -1, -2, 2\}$
45. $a_1 = \{0, 2, -2, -2\}, a_2 = \{0, 0, -1, 0\}, a_3 = \{0, 0, 2, 0\}, a_4 = \{-1, -1, 0, 2\},$
 $b_1 = \{2, -2, 1, -2\}, b_2 = \{-2, 1, -2, 0\}, b_3 = \{1, 2, 0, -2\}$
46. $a_1 = \{-2, -1, -2, 2\}, a_2 = \{1, -2, 0, -2\}, a_3 = \{1, 1, -1, 2\}, a_4 = \{-1, -1, 1, 0\},$
 $b_1 = \{1, -2, -2, 0\}, b_2 = \{0, 2, 2, -1\}, b_3 = \{-1, -1, -1, 2\}$
47. $a_1 = \{1, -1, 0, 1\}, a_2 = \{1, -1, -1, -1\}, a_3 = \{-2, 1, 0, 0\}, a_4 = \{-2, -1, 2, 2\},$
 $b_1 = \{0, 0, -1, -2\}, b_2 = \{-1, -1, -1, -2\}, b_3 = \{-1, 2, 1, -2\}$
48. $a_1 = \{2, 0, -1, -2\}, a_2 = \{-2, 0, 1, 2\}, a_3 = \{-2, 0, 0, 0\}, a_4 = \{0, 2, -1, 0\},$
 $b_1 = \{2, -2, 1, -2\}, b_2 = \{-2, -2, 0, 0\}, b_3 = \{0, 1, 2, 1\}$
49. $a_1 = \{2, 1, 1, -1\}, a_2 = \{2, -2, -1, -2\}, a_3 = \{1, 0, -2, 0\}, a_4 = \{-1, -2, 0, 0\},$
 $b_1 = \{2, -2, -2, 1\}, b_2 = \{-2, 0, 1, 2\}, b_3 = \{-1, -2, -2, 2\}$

50. $a_1 = \{-2, -2, -1, -1\}, a_2 = \{-2, 2, 2, -1\}, a_3 = \{-1, 0, 2, 0\}, a_4 = \{-1, 1, 1, 0\},$
 $b_1 = \{0, -2, 0, 2\}, b_2 = \{0, 2, -1, -1\}, b_3 = \{2, 2, 2, 0\}$
51. $a_1 = \{0, 1, 2, 0\}, a_2 = \{0, 2, 0, 1\}, a_3 = \{0, 1, -2, 1\}, a_4 = \{2, -1, 1, -1\},$
 $b_1 = \{1, -1, -1, 0\}, b_2 = \{1, 2, -1, 1\}, b_3 = \{-1, 2, 2, -2\}$
52. $a_1 = \{-1, -2, -2, 0\}, a_2 = \{-1, 2, -2, -2\}, a_3 = \{1, 0, 2, 0\}, a_4 = \{-2, -2, 2, 1\},$
 $b_1 = \{-2, 1, -1, 2\}, b_2 = \{-1, 1, -1, 1\}, b_3 = \{1, -1, 2, -2\}$
53. $a_1 = \{-2, -1, -2, 0\}, a_2 = \{-1, -1, 0, -1\}, a_3 = \{-2, -1, 2, -2\}, a_4 = \{2, 0, -1, -2\},$
 $b_1 = \{-2, 2, -2, 1\}, b_2 = \{-1, 0, 1, 1\}, b_3 = \{-2, -1, 0, 2\}$
54. $a_1 = \{2, -1, -2, -1\}, a_2 = \{1, -2, 0, 1\}, a_3 = \{0, 2, 2, 1\}, a_4 = \{2, 0, 0, 2\},$
 $b_1 = \{-2, -2, 2, 0\}, b_2 = \{1, 0, -1, 1\}, b_3 = \{0, 1, 2, -1\}$
55. $a_1 = \{0, -2, 1, 2\}, a_2 = \{1, 0, 2, 1\}, a_3 = \{-2, 1, -1, 0\}, a_4 = \{2, -1, -2, 2\},$
 $b_1 = \{-2, -2, 1, 0\}, b_2 = \{-2, 2, -1, 0\}, b_3 = \{2, -2, 1, 1\}$
56. $a_1 = \{-2, 2, 2, -1\}, a_2 = \{0, 0, 0, -1\}, a_3 = \{2, 0, -2, -2\}, a_4 = \{-2, -1, -1, 0\},$
 $b_1 = \{-1, 2, -2, -1\}, b_2 = \{1, 2, -1, -1\}, b_3 = \{0, -1, -2, -2\}$
57. $a_1 = \{2, 1, 0, -1\}, a_2 = \{1, 1, -2, 0\}, a_3 = \{0, -2, 2, 0\}, a_4 = \{1, -2, 1, -1\},$
 $b_1 = \{2, -2, -1, 2\}, b_2 = \{2, -2, 0, -2\}, b_3 = \{0, 0, 0, -2\}$
58. $a_1 = \{1, 2, 1, -1\}, a_2 = \{1, -2, -1, -1\}, a_3 = \{2, -2, -1, -2\}, a_4 = \{0, -1, 1, 1\},$
 $b_1 = \{-2, 0, 2, -2\}, b_2 = \{-1, -1, 0, 0\}, b_3 = \{1, 2, -1, -2\}$
59. $a_1 = \{-1, -2, 2, 1\}, a_2 = \{-2, 1, 0, 0\}, a_3 = \{1, 1, -2, 2\}, a_4 = \{2, -1, -1, 2\},$
 $b_1 = \{1, 1, 2, 2\}, b_2 = \{1, -2, -1, 0\}, b_3 = \{-2, 0, 1, -2\}$
60. $a_1 = \{-2, -1, 1, 1\}, a_2 = \{1, 2, 2, -1\}, a_3 = \{0, -2, -1, 0\}, a_4 = \{0, 0, 2, 2\},$
 $b_1 = \{1, -1, 1, 2\}, b_2 = \{-1, 2, -1, 1\}, b_3 = \{-1, -2, -2, -1\}$
61. $a_1 = \{-1, 1, -2, 1\}, a_2 = \{2, 1, 2, 0\}, a_3 = \{1, 1, 2, 1\}, a_4 = \{-1, 1, -1, 2\},$
 $b_1 = \{-1, -1, -1, 2\}, b_2 = \{0, 2, 2, 0\}, b_3 = \{1, 0, -2, -1\}$
62. $a_1 = \{1, 0, 0, -2\}, a_2 = \{2, 0, 0, -1\}, a_3 = \{1, -2, -2, -2\}, a_4 = \{2, 2, 0, 0\},$
 $b_1 = \{1, 1, 2, -1\}, b_2 = \{-2, 1, 1, -1\}, b_3 = \{1, -2, -1, -2\}$
63. $a_1 = \{1, 0, 0, 0\}, a_2 = \{0, 2, 0, -1\}, a_3 = \{-1, -1, 0, 1\}, a_4 = \{2, 1, -1, 2\},$
 $b_1 = \{1, -2, 2, -2\}, b_2 = \{-1, 1, 2, -2\}, b_3 = \{1, -1, -2, 2\}$
64. $a_1 = \{-1, -1, 2, 2\}, a_2 = \{2, -1, 0, 1\}, a_3 = \{1, -2, -2, -2\}, a_4 = \{-1, -2, 2, 0\},$
 $b_1 = \{0, 2, -2, 2\}, b_2 = \{-2, -2, 2, -1\}, b_3 = \{2, 1, -2, 0\}$
65. $a_1 = \{-1, -2, 1, 2\}, a_2 = \{-2, 2, -2, -1\}, a_3 = \{-2, 1, 2, 1\}, a_4 = \{1, -1, -2, 1\},$
 $b_1 = \{2, 0, -1, 2\}, b_2 = \{1, -2, 0, 1\}, b_3 = \{2, 1, 0, -1\}$
66. $a_1 = \{-2, -2, 1, 0\}, a_2 = \{2, 2, 1, 2\}, a_3 = \{1, -1, -2, -2\}, a_4 = \{1, 2, 1, 0\},$
 $b_1 = \{-2, 2, 2, -1\}, b_2 = \{2, -2, -1, -2\}, b_3 = \{-1, 1, -1, 0\}$
67. $a_1 = \{1, -2, -2, 1\}, a_2 = \{-1, -1, 0, -1\}, a_3 = \{2, 0, 1, 1\}, a_4 = \{-2, -2, 2, 2\},$
 $b_1 = \{1, 0, 2, 0\}, b_2 = \{-2, 0, 2, 1\}, b_3 = \{2, 2, -2, 2\}$

68. $a_1 = \{2, -2, 2, 1\}, a_2 = \{-2, 2, 0, 1\}, a_3 = \{1, 0, 0, 1\}, a_4 = \{-1, -1, -1, -2\},$
 $b_1 = \{-2, 0, -2, 1\}, b_2 = \{-2, -1, -1, -1\}, b_3 = \{-1, 2, -1, -1\}$
69. $a_1 = \{0, 2, 0, 2\}, a_2 = \{1, -2, -1, 2\}, a_3 = \{1, 1, -2, -2\}, a_4 = \{-1, 2, 2, -1\},$
 $b_1 = \{1, 0, 2, 0\}, b_2 = \{-2, -1, 2, -2\}, b_3 = \{1, 0, 1, 1\}$
70. $a_1 = \{2, 2, 1, 2\}, a_2 = \{-1, 2, -2, 0\}, a_3 = \{-2, 2, 1, -2\}, a_4 = \{1, 0, -1, -2\},$
 $b_1 = \{2, 1, -1, 0\}, b_2 = \{2, -1, 2, -1\}, b_3 = \{-2, 1, 2, -1\}$
71. $a_1 = \{0, 1, 1, 1\}, a_2 = \{1, 2, 1, 2\}, a_3 = \{-1, 0, 2, 0\}, a_4 = \{0, 2, 2, -1\},$
 $b_1 = \{-2, 2, 2, -2\}, b_2 = \{-2, 0, 0, 1\}, b_3 = \{1, 0, 2, 2\}$
72. $a_1 = \{1, -2, 2, 1\}, a_2 = \{1, 1, 1, 2\}, a_3 = \{-1, 2, 2, 0\}, a_4 = \{-1, 2, 0, 1\},$
 $b_1 = \{0, 2, -2, -1\}, b_2 = \{1, 0, -1, 0\}, b_3 = \{0, 2, -2, 0\}$
73. $a_1 = \{0, -2, 0, 0\}, a_2 = \{0, 0, 0, -1\}, a_3 = \{2, 2, 1, -1\}, a_4 = \{-1, 2, 1, -2\},$
 $b_1 = \{-2, -2, 0, -1\}, b_2 = \{-1, 2, 1, -2\}, b_3 = \{0, 1, 1, 0\}$
74. $a_1 = \{2, 1, -1, -2\}, a_2 = \{-2, -1, 0, -1\}, a_3 = \{0, -1, 2, 2\}, a_4 = \{1, -1, 1, 2\},$
 $b_1 = \{-2, -1, 1, -1\}, b_2 = \{1, 2, 0, 1\}, b_3 = \{-2, 2, -2, 1\}$
75. $a_1 = \{0, -2, 1, 2\}, a_2 = \{2, -2, -1, -2\}, a_3 = \{-2, 0, 2, 0\}, a_4 = \{-2, 1, 0, 0\},$
 $b_1 = \{-1, -2, 0, 1\}, b_2 = \{2, -1, 2, 1\}, b_3 = \{-2, 0, -1, 1\}$
76. $a_1 = \{1, 1, 0, -1\}, a_2 = \{2, 0, 2, -2\}, a_3 = \{0, 2, 1, -1\}, a_4 = \{2, 1, 1, 0\},$
 $b_1 = \{1, 1, -2, 0\}, b_2 = \{-2, 2, 0, 2\}, b_3 = \{-1, -1, 2, 2\}$
77. $a_1 = \{-2, -1, -2, 2\}, a_2 = \{1, -1, 1, -2\}, a_3 = \{2, -1, 0, 0\}, a_4 = \{1, -2, -1, -2\},$
 $b_1 = \{2, 0, -1, 0\}, b_2 = \{2, 2, -2, -2\}, b_3 = \{1, 2, 2, -1\}$
78. $a_1 = \{2, -2, -1, 1\}, a_2 = \{2, 0, 1, -1\}, a_3 = \{-2, 0, 2, 2\}, a_4 = \{1, 1, 2, 1\},$
 $b_1 = \{2, 1, -2, -2\}, b_2 = \{-1, 0, -2, -1\}, b_3 = \{-2, 2, 2, -2\}$
79. $a_1 = \{-2, 1, -2, 1\}, a_2 = \{-1, -1, 0, -2\}, a_3 = \{-1, 2, -1, -2\}, a_4 = \{1, -1, 0, 0\},$
 $b_1 = \{2, 0, -1, 2\}, b_2 = \{-2, 0, 0, -1\}, b_3 = \{2, -2, 0, -1\}$
80. $a_1 = \{0, 0, 2, 1\}, a_2 = \{1, -2, -1, -2\}, a_3 = \{0, -1, 1, 2\}, a_4 = \{1, -1, 1, 1\},$
 $b_1 = \{2, 1, -2, 1\}, b_2 = \{-1, 0, -1, 2\}, b_3 = \{1, 0, 2, 0\}$
81. $a_1 = \{-1, -1, 0, -1\}, a_2 = \{-1, -1, -1, -2\}, a_3 = \{0, 1, 1, 1\}, a_4 = \{-1, 1, -1, 1\},$
 $b_1 = \{-1, 0, 0, 2\}, b_2 = \{-2, -1, 2, -2\}, b_3 = \{-2, -1, -1, 1\}$
82. $a_1 = \{1, 1, -1, -1\}, a_2 = \{0, 2, -1, -1\}, a_3 = \{-2, -1, 1, 2\}, a_4 = \{-2, -1, -1, -1\},$
 $b_1 = \{1, 1, 2, -1\}, b_2 = \{-2, -1, -1, 2\}, b_3 = \{2, 2, -1, 2\}$
83. $a_1 = \{1, -1, 0, 0\}, a_2 = \{2, 0, -1, -2\}, a_3 = \{1, 1, 2, 0\}, a_4 = \{1, 2, 1, 2\},$
 $b_1 = \{-2, -1, 2, 0\}, b_2 = \{-1, 0, 0, 0\}, b_3 = \{-2, 1, -2, -1\}$
84. $a_1 = \{0, 0, -2, 2\}, a_2 = \{-1, 0, 1, 2\}, a_3 = \{-1, -1, 0, -1\}, a_4 = \{2, 2, 0, -1\},$
 $b_1 = \{0, -1, 1, -1\}, b_2 = \{-1, -2, -2, -1\}, b_3 = \{2, 1, 0, -1\}$
85. $a_1 = \{-2, -2, -1, 0\}, a_2 = \{2, 0, 2, 2\}, a_3 = \{-2, 0, -2, 1\}, a_4 = \{-2, -2, -1, -1\},$
 $b_1 = \{1, 1, -1, 1\}, b_2 = \{-2, -2, -2, 1\}, b_3 = \{0, 1, -1, -2\}$

86. $a_1 = \{1, 1, 0, 0\}, a_2 = \{0, -2, -1, 0\}, a_3 = \{2, 2, -1, -1\}, a_4 = \{-2, 1, 2, 2\},$
 $b_1 = \{2, 2, 0, 1\}, b_2 = \{-2, 0, -2, 0\}, b_3 = \{-2, 2, 0, 2\}$
87. $a_1 = \{0, -1, 2, -2\}, a_2 = \{2, 1, 1, 2\}, a_3 = \{-1, 1, 1, -2\}, a_4 = \{-1, 2, -1, 2\},$
 $b_1 = \{-1, 1, -1, -2\}, b_2 = \{-2, 1, 0, -2\}, b_3 = \{2, 1, 1, -2\}$
88. $a_1 = \{-1, -1, 1, 2\}, a_2 = \{-2, -2, 1, 1\}, a_3 = \{0, -2, 2, 1\}, a_4 = \{-1, -2, -2, -2\},$
 $b_1 = \{-1, -2, 2, 2\}, b_2 = \{-2, 0, 0, 1\}, b_3 = \{1, 0, 1, 2\}$
89. $a_1 = \{2, -1, 0, 2\}, a_2 = \{-2, -1, 2, -2\}, a_3 = \{1, 2, 1, -1\}, a_4 = \{-2, 1, 2, -2\},$
 $b_1 = \{0, 1, -1, 1\}, b_2 = \{-1, -1, 1, 2\}, b_3 = \{-2, 0, 0, -1\}$
90. $a_1 = \{0, 1, 0, 2\}, a_2 = \{0, 0, 0, 0\}, a_3 = \{0, -1, 1, 1\}, a_4 = \{1, 0, 1, -2\},$
 $b_1 = \{0, -2, 2, 0\}, b_2 = \{-2, -1, 2, 2\}, b_3 = \{2, 0, 1, 0\}$
91. $a_1 = \{0, 2, -2, -2\}, a_2 = \{-1, 0, 2, 2\}, a_3 = \{2, -1, 0, 0\}, a_4 = \{-1, 2, 1, 2\},$
 $b_1 = \{-2, -2, -2, -1\}, b_2 = \{2, -1, 0, 0\}, b_3 = \{-1, 1, 1, -1\}$
92. $a_1 = \{2, -1, -2, 2\}, a_2 = \{-2, 2, 0, 0\}, a_3 = \{1, 1, -2, 2\}, a_4 = \{0, -2, 0, 1\},$
 $b_1 = \{0, -2, 1, 1\}, b_2 = \{-1, 2, -2, 2\}, b_3 = \{0, -2, 1, 0\}$
93. $a_1 = \{-2, -2, -1, -1\}, a_2 = \{-2, 1, 0, 0\}, a_3 = \{-2, -2, 2, -1\}, a_4 = \{-2, -1, 0, -2\},$
 $b_1 = \{-1, 2, 2, -1\}, b_2 = \{0, 0, -2, 2\}, b_3 = \{-1, -2, 2, 1\}$
94. $a_1 = \{-1, 1, 2, -1\}, a_2 = \{1, 1, -2, -1\}, a_3 = \{-2, -1, 1, -2\}, a_4 = \{0, 0, 1, -1\},$
 $b_1 = \{2, -1, -1, 2\}, b_2 = \{-2, 1, 2, -2\}, b_3 = \{-1, 2, 2, -2\}$
95. $a_1 = \{2, -1, 1, 2\}, a_2 = \{1, 1, 0, 0\}, a_3 = \{0, -1, 2, 0\}, a_4 = \{1, -2, -1, 1\},$
 $b_1 = \{-2, 0, -2, 2\}, b_2 = \{2, 0, 0, 1\}, b_3 = \{1, 2, 2, 0\}$
96. $a_1 = \{0, -1, 2, 2\}, a_2 = \{-1, 0, 1, -2\}, a_3 = \{2, 1, 0, 0\}, a_4 = \{0, -2, 1, -1\},$
 $b_1 = \{-2, -2, 0, -1\}, b_2 = \{-2, 1, 2, -1\}, b_3 = \{2, 0, -1, -2\}$
97. $a_1 = \{-1, -2, 2, 0\}, a_2 = \{0, 1, 0, -1\}, a_3 = \{0, 0, 0, 0\}, a_4 = \{2, 2, -1, -2\},$
 $b_1 = \{2, 1, 0, -1\}, b_2 = \{-2, 2, 1, 1\}, b_3 = \{0, -1, 2, 0\}$
98. $a_1 = \{-1, 2, -2, -1\}, a_2 = \{2, 1, -2, -1\}, a_3 = \{2, 0, 2, 2\}, a_4 = \{-1, -1, 1, 0\},$
 $b_1 = \{-2, -2, 1, -1\}, b_2 = \{1, 0, 0, -2\}, b_3 = \{0, 1, -2, 0\}$
99. $a_1 = \{1, -2, -2, 2\}, a_2 = \{0, -1, 0, 1\}, a_3 = \{-2, -1, 0, -2\}, a_4 = \{2, -1, 0, 1\},$
 $b_1 = \{-1, -2, -1, -1\}, b_2 = \{0, 0, -1, 1\}, b_3 = \{-2, -2, -1, 2\}$
100. $a_1 = \{0, -2, 1, -2\}, a_2 = \{-2, 0, 0, 0\}, a_3 = \{2, 1, -1, -1\}, a_4 = \{-1, 2, 1, 1\},$
 $b_1 = \{-2, 2, -1, -1\}, b_2 = \{-1, -2, 0, -1\}, b_3 = \{-1, 2, -2, 1\}$